# Crystallization behaviour of a semicrystalline miscible blend

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A theoretical model has been developed to explain the crystallization behaviour in a thermodynamically miscible blend of a semicrystalline and amorphous polymer. The model predicts the growth rate and half-time for the maximum crystallization, and relates the observable melting temperatures to the equilibrium melting temperatures in each blend. A complete equation that contains morphological, entropic and enthalpic contributions has been developed for this purpose.

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## **INTRODUCTION**

Scientific and industrial interest in polymer blends has been gaining steady and significant momentum in the past few years. A market growth of 9% each year until 1996 has been forecast by Kossoff and Associates<sup>1</sup> for thermoplastic polymer blends. From a scientific point of view, however, polymer blends can be divided into three basic groups:

Group 1	Miscible blends, such as: PPO-PS PVDF-PMMA
Group 2	Near-miscible blends, such as PS-PVME PES-PEO PVC-PBA

Group 3 Immiscible blends, such as: PE-PMMA PP-PC

The above abbreviations and the mathematical symbols used here are defined in the 'Notation' at the end of the paper.

Miscibility is defined by a single  $T_g$  and  $\partial^2 \Delta G / \partial \phi^2 > 0$ . The group 1 blends do not show a phase separation within the accessible temperature ranges, whereas the blends in group 2 show a detectable phase transition of predominantly lower critical solution temperature (LCST) type. The miscibility is a result of a favourable combination of two sets of quantities: (a) the match between physical quantities such as volumes and expansion coefficients and (b) chemical structures that allow a specific interaction to occur between the functional groups of the blend constituents. The latter is generally more important in high-molecular-weight polymeric mixtures than the former. In the absence of these favourable parameters, a mixture of two polymers will be heterogeneous with two  $T_g$  values.

The structure-property relationships in these three groups of polymeric blends are different. In the majority of cases miscible blends provide the ultimate properties that one would hope to achieve from blending practice.

The high-performance and engineering thermoplastics

used in applications normally contain a certain level of crystallinity. The crystallinity region provides hightemperature strength and environmental resistance for the polymer. It is therefore important to know how the crystals are affected when a semicrystalline polymer is blended with an amorphous one that has favourable interactions. The aim of this paper is to explain, theoretically, the crystallinity behaviour of such a mixture.

#### BACKGROUND TO THE SUBJECT

The addition of an amorphous polymer to a semicrystalline polymer, which forms a thermodynamically miscible blend, has a dramatic effect on the crystallization behaviour of the latter. Ullman  $et al.^2$  have shown that the lamellar thickness of poly(vinylidene fluoride) (PVDF) blended with poly(methyl methacrylate) (PMMA) decreases as the concentration of PMMA increases. The thickness of the amorphous layer and the long period increase as PMMA concentration increases. Cimmino et  $al.^3$  have shown that the spherulite radial growth rate of poly(ethylene oxide) (PEO) decreases, and its half-time of crystallization increases at a given crystallization temperature, when it is blended with PMMA or poly(vinyl acetate) (PVAc). Various authors<sup>4-6</sup> have reported an observable depression on the melting of crystals in miscible blends. Alfonso et al.<sup>7</sup> reported that the kinetics and the thermodynamic parameters governing the crystallization of blends need modification.

Given the above information, there is no comprehensive theoretical model available to explain these observations. Sanchez *et al.*<sup>8</sup> have offered a theoretical model with various degrees of approximations for crystallization behaviour from a dilute solution. Flory<sup>9</sup> has related the observable melting-point depression to entropy and enthalpy of the crystalline units in the mixtures. This equation has been widely used but was found to be inadequate for describing the melting-point depression in blends<sup>7,10</sup>

In this paper a more comprehensive model describing the crystallization behaviour of a semicrystalline polymer Crystallization of a miscible blend: S. Rostami



Figure 1 Schematic presentation of crystalline/amorphous regions of a homopolymer with and without the other component. The symbols are defined in the 'Notation'. The amorphous polymer (A) is referred to as component 1, and the semicrystalline polymer as component 2

in the presence of an amorphous polymer is presented. The observable melting point is related to an equilibrium melting point in each blend. These treatments are only valid when the two components are thermodynamically miscible. The semicrystalline component is generally referred to as component 2 and the amorphous polymer as component 1. Component 1 (*Figure 1*) is excluded from the crystalline region. The symbols used in this figure are defined in the 'Notation'.

#### THE EQUILIBRIUM MELTING TEMPERATURE IN BLENDS

In a semicrystalline homopolymer the change in free energy of melting per mole of crystalline unit is given by:

$$\Delta G_{\rm u}(T) = \Delta H_{\rm u} - T \Delta S_{\rm u} \tag{1}$$

where  $\Delta H_u$  and  $\Delta S_u$  are heat of fusion and entropy changes on melting. For an infinitely large crystal with an equilibrium melting temperature of  $T_m^*$  then  $\Delta G_u(T_m^*) = 0$  or:

$$T_{\rm m}^* = \Delta H_{\rm u} / \Delta S_{\rm u} \tag{2}$$

Assuming  $\Delta S$  is constant over the temperature range of  $T_{\rm m}$  to  $T_{\rm m}^*$  then equation (1) can be written as:

$$\Delta G_{\rm u}(T_{\rm m}) = \Delta H_{\rm u} - T_{\rm m} \left( \frac{\Delta H_{\rm u}}{T_{\rm m}^*} \right) = \Delta H_{\rm u} \left( \frac{T_{\rm m}^* - T_{\rm m}}{T_{\rm m}^*} \right) \quad (3)$$

Also at  $T_{\rm m}$ :

$$n\Delta G_{\rm u}(T_{\rm m}) = 2\sigma_{\rm e} \tag{4}$$

Combining equations (3) and (4) gives:

$$T_{\rm m} = T_{\rm m}^* \left( 1 - \frac{2\sigma_{\rm e}}{\Delta H_{\rm u} n} \right) \tag{5}$$

This equation often appears in the literature and relates the observable melting to the equilibrium melting temperatures in homopolymers. Blundell *et al.*<sup>11</sup> have used this equation to calculate the equilibrium melting temperature of poly(ether ether ketone) (PEEK).

For blends, however, the difference in free energy of the crystalline unit can be written as<sup>8</sup>:

$$n\Delta G_{\rm ub}(T) = n\Delta G_{\rm u}(T) + \Delta G_{\rm M} \tag{6}$$

$$\Delta G_{ub}(T) = \Delta H_u - T \Delta S_u + \Delta g_M \tag{7}$$

where the heat of fusion of the crystalline unit in the blend is assumed to be equal to that of the homopolymer. If we start with an athermal mixture, where the heat of mixing is zero, then equation (7) becomes:

$$\Delta G_{ub}(T) = \Delta H_u - T \Delta S_u - T \Delta S_M \tag{8}$$

At  $T = T^*_{mb}$  we have:

$$T_{\rm mb}^* = \Delta H_{\rm u} / \Delta S_{\rm ub} \tag{9}$$

where

$$\Delta G_{ub}(T_{mb}) = \Delta H_u \left(1 - \frac{T_{mb}}{T_{mb}^*}\right) - T_{mb} \Delta s_M \qquad (10)$$

As in equation (4):

$$\Delta G_{\rm ub}(T_{\rm mb}) = 2(\sigma_{\rm e}/n)_{\rm b} \tag{11}$$

By combining equations (10) and (11) and rearranging we have:

$$\frac{1}{T_{\rm mb}} = \left(\frac{1}{T_{\rm mb}^*} + \frac{\Delta s_{\rm M}}{\Delta H_{\rm u}}\right) \left(\frac{1}{1 - (2\sigma_{\rm eb}/\Delta H_{\rm u}n_{\rm b})}\right) \qquad (12)$$

This equation relates the observable melting temperature to the equilibrium melting temperature in athermal polymer blends. It is shown by Cimmino<sup>3</sup> and Ullman<sup>2</sup> that:

$$\sigma_{\mathbf{e}\mathbf{b}} = \phi_1^{\alpha} \sigma_{\mathbf{e}} \qquad n_{\mathbf{b}} = (1 - \phi_1)^{\beta} n \qquad (13)$$

where  $\alpha$  and  $\beta$  are constants and need to be evaluated for each system.

In equation (12) if  $\Delta s_{\rm M} \rightarrow 0$  then:

$$T_{\rm mb} = T_{\rm mb}^* \left( 1 - \frac{2\sigma_{\rm e}}{\Delta H_{\rm u} n_{\rm b}} \right) \tag{14}$$

If the heat of mixing of the amorphous region is not ignored, then equation (7) with a similar treatment as that of equation (12) gives:

$$T_{\rm mb} = T_{\rm mb}^* \left( 1 - \frac{2\sigma_{\rm eb}}{\Delta H_{\rm u} n_{\rm b}} + \frac{\Delta g_{\rm M}}{\Delta H_{\rm u}} \right) \tag{15}$$

where the  $\Delta g_{\rm M}$  is the difference in free energy per mole of crystalline unit between amorphous and crystalline polymer. Equation (15) is a general form of the equation that relates the observable melting temperature to the equilibrium melting temperature of the blend. This equation will be expanded in the following sections to explain the crystallization behaviour of the blend.

#### THE SPHERULITIC GROWTH RATE

The common equation used to describe the radial growth rate of a semicrystalline polymer is given by Hoffman *et* al.<sup>12</sup> as:

$$G = G^{0} \exp\left(-\frac{C_{1}}{T - T_{g} + C_{2}}\right) \exp\left(-\frac{4\sigma_{e}\sigma_{0}}{RT}\frac{1}{\Delta G_{u}(T)}\right) (16)$$

where  $G^0$  is a pre-exponential factor that is inversely proportional to  $\overline{M}_n$  of the polymer<sup>13</sup>. The other two terms describe kinetic and energetic parts of the growth rate respectively.  $C_1$  and  $C_2$  are constants and will be defined later.  $\sigma_e \sigma_0$  is the product of the fold and lateral free energies<sup>12</sup>.

Using equations (3) and

$$C_3 = 4\sigma_{\rm e}\sigma_0/R\Delta H_{\rm u}$$

this equation becomes:

$$G = G^{0}(\bar{M}_{n}) \exp\left(-\frac{C_{1}}{T - T_{g} + C_{2}}\right) \exp\left(-\frac{C_{3}T_{m}^{*}}{T(T_{m}^{*} - T_{m})}\right)$$
(17)

For the crystalline unit in the blend, however, it becomes:

$$G_{b} = G_{b}^{0}(\bar{M}_{n}) \exp\left(-\frac{C_{1}}{T - T_{gb} + C_{2}}\right) \times \exp\left(-\frac{C_{4}T_{mb}^{*}}{T[T_{mb}^{*} - T_{m} + T_{mb}^{*}(\Delta g_{M}/\Delta H_{u})]}\right)$$
(18)

where

$$C_4 = 4(\sigma_{\rm e}\sigma_{\rm 0})_{\rm b}/R\Delta H_{\rm u}$$

For a miscible blend where  $\Delta g_M < 0$ , equation (18) indicates a slower rate of spherulitic growth in the blend than that of the homopolymer. This has been shown experimentally by Cimmino for various PEO blends. According to this equation the radial growth rate should continue to decrease as the concentration of the amorphous polymer increases. It is conceivable that at some value of  $\Delta g_M$ , where the thermodynamic miscibility is preferred, the last term in equation (18) vanishes and crystal growth ceases.

For an athermal mixture the radial growth rate is similarly given by:

$$G_{\rm b} = G_{\rm b}^{0}(\bar{M}_{\rm n}) \exp\left(-\frac{C_{1}}{T - T_{\rm gb} + C_{2}}\right) \\ \times \exp\left(-\frac{C_{4}T_{\rm mb}^{*}}{T[T_{\rm mb}^{*} - T_{\rm m} - (TT_{\rm m}^{*}\Delta s_{\rm m}/\Delta H_{\rm u})]}\right)$$
(19)

In this equation  $-T\Delta s_{\rm M}$  is also negative, which implies that the growth in such a mixture is also slower than the crystallizable homopolymer component.

The values of  $C_1$  and  $C_2$  for miscible blends with a single  $T_g$  are given by a WLF equation, where:

$$\log a_{T} = \log\left(\frac{\eta_{T}}{\eta_{T_{g}}}\right) = \frac{B}{2.303} \left(\frac{1}{f(T)} - \frac{1}{f(T_{g})}\right)$$
(20)

$$f(T) = f(T_{g}) + \Delta \alpha (T - T_{g})$$
(21)

$$C_1 = \frac{B(T - T_g)}{2.303f(T_g)} \simeq 450 \text{ (K)} \qquad C_2 = \frac{f(T_g)}{\Delta \alpha} \simeq 52 \text{ (K)} \quad (22)$$

Hence

$$\log a_T = \frac{-C_1}{T - T_{gb} + C_2}$$
(23)

This principle is expected to be applicable for a miscible blend although the  $C_1$  and  $C_2$  values could vary slightly. Alfonso *et al.*<sup>7</sup> have derived an expression, based on the diffusion of the two polymers, to replace the transport factor.

# THE CRYSTALLIZATION TIME IN THE BLEND

Ullman et  $al.^2$  have shown that the total level of crystallinity in the blends decreases exponentially as the concentration of the amorphous polymer increases. The time to achieve such a level of crystallinity can be obtained from Avrami equations:

$$W_{\rm cb} = W_{\rm max} \left[ 1 - \exp\left( -\frac{4\pi}{3} N_{\rm 0b} G_{\rm b}^3 (t - t_0)^m \right) \right] \quad (24)$$

The nuclei density,  $N_{0b}$ , varies with the temperature and molecular dimension of the crystallizable unit.  $t_0$  is the induction time. At  $t = t_{1/2}$  where  $W_{cb} = \frac{1}{2}W_{max}$  and for m = 3 we have:

$$(t_{1/2})_{\rm b} = \frac{1}{G_{\rm b}} \left( \frac{3 \ln 2}{4\pi N_{\rm 0b}} \right)^{1/3} + t_0 \tag{25}$$

where  $G_b$  is given by equation (18). The slower spherulitic growth rates, as mentioned earlier, imply that longer times are required to reach half of the maximum crystallization in the blend compared with that of the homopolymer.  $(t_{1/2})_b$  and  $G_b$  for blends are compositiondependent and from equation (25) it appears that  $G_b$  is concentration-dependent too. However, for each blend composition  $G_b$  decreases linearly with  $(t_{1/2})_b$ , as shown by Van Antwerppen<sup>13</sup> for poly(ethylene terephthalate) (PET).

#### EVALUATION OF $\Delta g_{M}$ AND $\Delta s_{M}$

According to standard thermodynamic practice  $\Delta g_{\rm M}$  is equivalent to the change in chemical potential per mole of crystalline unit. This is given by Flory<sup>9</sup> using his lattice model as:

$$\Delta \mu_{2u} = \frac{RTV_{u}}{V_{1}} \left[ \frac{\ln \phi_{2}}{r_{2}} + \left( \frac{1}{r_{2}} - \frac{1}{r_{1}} \right) \phi_{1} \right] + \frac{RTV_{u}}{V_{1}} \chi_{12} \phi_{1}^{2} \quad (26)$$

For an athermal mixture where  $\chi_{12} = 0$  equation (26) becomes:

$$-T\Delta s_{\rm M} = \frac{RTV_{\rm u}}{V_1} \left[ \frac{\ln \phi_2}{r_2} + \left( \frac{1}{r_2} - \frac{1}{r_1} \right) \phi_1 \right]$$
(27)

At extremely low concentrations of amorphous polymer where  $\phi_1 \rightarrow 0$  it reduces to:

$$-T\Delta s_{\rm M} \simeq \frac{RT}{r_2} \frac{V_{\rm u}}{V_1} \ln \phi_2 \tag{28}$$

This is the change in the entropy of athermal mixtures which often appears in the literature. However, substituting equation (28) into equation (12) gives:

$$\frac{1}{T_{\rm mb}} = \left(\frac{1}{T_{\rm mb}^*} - \frac{RV_{\rm u}}{r_2 V_1} \ln \phi_2\right) \left(1 - \frac{2\sigma_{\rm eb}}{\Delta H_{\rm u} n_b}\right)^{-1}$$
(29)

Equation (29) is only applicable to athermal mixtures. For non-athermal mixtures the complete version of equation (26) should be used. The  $\chi_{12}$  interaction parameter in this equation is concentration, temperature and pressure dependent. It seems advantageous to replace this parameter by an alternative interaction parameter, namely  $X_{12}$ , which is concentration-independent.  $X_{12}$  is still temperature- and pressure-dependent. According to Flory's equation-of-state theory<sup>14</sup>:

$$\Delta \mu_{2u} = \Delta \mu_{2u}^{\text{comb}} + \Delta \mu_{2u}^{\text{res}}$$
(30)

where

$$\Delta \mu_{2}^{\text{res}} = RT \chi_{12} \phi_{1}^{2}$$

$$= P_{2}^{*} V_{2}^{*} \left[ 3\tilde{T}_{2} \ln \left( \frac{\tilde{v}_{2}^{1/3} - 1}{\tilde{v}^{1/3} - 1} \right) + \frac{1}{\tilde{v}_{2}} - \frac{1}{\tilde{v}} + \tilde{P}_{2}(\tilde{v} - \tilde{v}_{2}) \right]$$

$$+ \frac{V_{2}^{*} \theta_{1}^{2}}{\tilde{v}} \frac{S_{2}}{S_{1}} \left( X_{12} - T \tilde{v} Q_{12} \right)$$
(31)

For details of derivations and applications of this equation see refs. 14 and 15. Substituting equation (31) in equation (26) and the resultant into equation (15) and

Table 1	The	$Q_{12}$	and	$X_{12}$	ratio
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Blend	$X_{12} (\text{J cm}^{-3})$	$Q_{12} \times 10^{-3} \text{ (J cm}^{-3} \text{ K}^{-1})$	$Q_{12} \times 10^{-3} / X_{12}  (\mathrm{K}^{-1})$	Ref.
DPS-PVME	-1.86	-3.00	1.6	16
CPE-EVA	-4.20	-10.80	2.5	17
CPE-PBA	-1.01	-2.63	2.6	17
PVC-PMMA	-3.04	-6.08	2.0	17
PVC-PBA	-12.80	-25.60	2.0	18
PVC-PPrA	-15.11	- 30.00	2.0	18
PVC-PPeA	10.47	-22.00	2.0	18
PES-Phenoxy	-1.5	-2.70	1.8	19
PES-PEO	-40.00	-48.20	1.2	7



Figure 2 The chemical potential changes per mole of PEO in the mixtures of PES-PEO at  $25^{\circ}C$ 

rearranging gives:

$$T_{\rm mb} = T_{\rm mb}^{*} \left( 1 - \frac{2\sigma_{\rm eb}}{\Delta H_{\rm u} n_{\rm b}} \right) + \frac{T_{\rm mb}^{*}}{\Delta H_{\rm u}} \frac{RTV_{\rm u}}{V_{\rm 1}} \left[ \frac{\ln \phi_{2}}{r_{2}} + \left( \frac{1}{r_{2}} - \frac{1}{r_{\rm 1}} \right) \phi_{\rm 1} \right] + \frac{T_{\rm mb}^{*}}{\Delta H_{\rm u}} \frac{V_{\rm u}}{V_{\rm 1}} P_{2}^{*} V_{2}^{*} \left[ 3\tilde{T}_{2} \ln \left( \frac{\tilde{v}_{2}^{1/3} - 1}{\tilde{v}^{1/3} - 1} \right) + \frac{1}{\tilde{v}_{2}} - \frac{1}{\tilde{v}} + \tilde{P}_{2}(\tilde{v} - \tilde{v}_{2}) \right] + \frac{T_{\rm mb}^{*}}{\Delta H_{\rm u}} \frac{V_{\rm u}}{V_{\rm 1}} \frac{V_{2}^{*}}{\tilde{v}} \frac{\theta_{1}^{2}S_{2}}{S_{1}} \left( X_{12} - T\tilde{v}Q_{12} \right)$$
(32)

This equation relates the observable melting temperature to the equilibrium melting temperature of a crystalline unit in the blend at atmospheric pressure,  $\tilde{P}_2 \approx 0$ , or at any given pressure. The first term in this equation is related to the morphology of the crystals in the blend, the second term is the change in combinatorial entropy of the mixture and the last two terms are related to entropy and enthalpy of the interactions. The numerical solutions of these two terms are given by Rostami *et al.*<sup>15</sup>. These two terms vanish as the heat of the mixing goes to zero.

The concentration-independent quantity,  $X_{12}$ , is related to the heat of mixing via:

$$\Delta H_{\rm m} = (\omega_1 v_{1\rm sp}^* + \omega_2 v_{2\rm sp}^*) \left( \frac{\phi_1 P_1^*}{\tilde{v}_1} + \frac{\phi_2 P_2}{\tilde{v}_2} - \frac{P^*}{\tilde{v}} \right)$$
(33)

where

$$P^* = \phi_1 P_1^* + \phi_2 P_2^* - \phi_1 \theta_2 X_{12} \tag{34}$$

The  $X_{12}$  value is normally obtained by measuring the heat of mixing of oligometric analogues in a microcalorimeter and using equations (33) and (34) to obtain a value of  $X_{12}$ .

The  $Q_{12}$  factor, however, arises from the entropy of interactions in the amorphous region. Data for  $X_{12}$  and  $Q_{12}$  for some polymeric blend systems cited in the literature are listed in *Table 1*. From this table the ratio between  $X_{12}$  and  $Q_{12}$  seems to be constant, leading to an empirical relation:

$$Q_{12} \simeq 2.0 \times 10^{-3} X_{12} \text{ K}^{-1}$$
 (35)

Using the values of  $X_{12}$  and  $Q_{12}$  given in this table and other required information given in ref. 6 the  $\Delta \mu_{2u}/RT$ of PES-PEO has been calculated for room temperature. The result is plotted in *Figure 2*.

## THE MELTING-POINT DEPRESSION IN BLENDS

Although there is some ambiguity in the definition of the observable crystalline melting temperature<sup>20</sup>, nevertheless many authors<sup>2-4,9,16,20</sup> have reported detectable differences between the melting behaviour of a semicrystalline polymer on its own and its blend. Almost invariably in all cases the observable melting point of the semicrystalline homopolymer is generally depressed in the blends. Equation (36) given by Flory<sup>9</sup> has been widely used to describe this behaviour. It has also been used to obtain the usual Flory-Huggins interaction parameter:

$$\frac{1}{\phi_1} \left( \frac{1}{T_{\rm mb}} - \frac{1}{T_{\rm m}} \right) = \frac{RV_{\rm u}}{\Delta H_{\rm u}V_1} \left( 1 - \chi_{12}\phi_1 \right)$$
(36)

Many authors have experienced difficulties in fitting this equation to their experimental data<sup>5,7,10</sup>. The principal difficulties are:

(1) This equation has been derived at conditions of observable melting temperatures, not at thermodynamic equilibrium temperatures.

(2) The plot of the left-hand side of equation (36) versus the right-hand side has an intercept with the y axis that contains information on the crystalline morphology<sup>5</sup> but has been ignored.

(3) The concentration dependence of the interaction parameter adds a restriction on plotting the left-hand side of equation (36) versus  $\phi_1$  to obtain a single value for  $\chi_{12}$ .

A modified version of this equation has been used by other authors $^{4,6}$  with an added constant factor that is

related to the morphology of the crystalline region. These approaches have not been entirely satisfactory.

Equation (32) contains all the necessary ingredients needed to explain the melting-point depression of the crystalline unit in the blends. It takes into account the morphology of the crystalline units, residual and combinatorial entropies and the enthalpy of mixing of a semicrystalline polymer with an amorphous one. At  $T = T_{mb}$  this equation can be rearranged to give:

$$\Delta H_{u} \left( \frac{1}{T_{mb}} - \frac{1}{T_{mb}^{*}} \right) = -\frac{RV_{u}}{V_{1}} \left[ \frac{\ln \phi_{2}}{r_{2}} + \left( \frac{1}{r_{2}} - \frac{1}{r_{1}} \right) \phi_{1} \right] - \frac{P_{2}^{*} V_{2}^{*}}{T_{mb}} \frac{V_{u}}{V_{1}} \left[ 3\tilde{T}_{2} \ln \left( \frac{\tilde{v}_{2}^{1/3} - 1}{\tilde{v}^{1/3} - 1} \right) + \frac{1}{\tilde{v}_{2}} - \frac{1}{\tilde{v}} + \tilde{P}_{2}(\tilde{v} - \tilde{v}_{2}) \right] - \frac{V_{2}^{*} V_{u}}{T_{mb}} \frac{\theta_{1}^{2}}{\tilde{v}} \frac{S_{2}}{S_{1}} \left( X_{12} - T_{mb} \tilde{v} Q_{12} \right) + \frac{1}{T_{mb}} \frac{2\sigma_{eb}}{\Delta H_{u} n_{b}}$$
(37)

This equation relates the observable melting point to the equilibrium melting point via four terms: first the morphological term, second the combinatorial entropy, third the residual entropy and fourth the enthalpic term. Verification of this equation requires a careful d.s.c., X-ray diffraction and calorimetric analysis of the semicrystalline blends.

In a specific situation where  $\sigma_{eb} = \sigma_e$ ,  $n_b = n$  and  $T^*_{mb} = T^*_m$  equation (37) reduces to:

$$\Delta H_{u} \left( 1 - \frac{T_{mb}}{T_{m}^{*}} \right) = \left( 1 - \frac{T_{m}}{T_{m}^{*}} \right)$$
$$- \frac{R T_{mb} V_{u}}{V_{1}} \left[ \frac{\ln \phi_{2}}{r_{2}} + \left( \frac{1}{r_{2}} - \frac{1}{r_{1}} \right) \phi_{1} \right]$$
$$- \frac{P_{2}^{*} V_{2}^{*} V_{u}}{V_{1}} \left[ 3 \tilde{T}_{2} \ln \left( \frac{\tilde{v}_{2}^{1/3} - 1}{\tilde{v}^{1/3} - 1} \right) + \frac{1}{\tilde{v}_{2}} - \frac{1}{\tilde{v}} + \tilde{P}_{2} (\tilde{v} - \tilde{v}_{2}) \right]$$
$$- \frac{V_{2}^{*} V_{u}}{V_{1}} \frac{\theta_{1}^{2}}{2} \frac{S_{2}}{2} \left( X_{e} - T_{e} \tilde{v} \theta_{1} \right)$$
(38)

$$V_1 \quad \tilde{v} S_1 \quad (12) \quad (00)$$
  
is simpler than equation (37) but assumes equal

which is simpler than equation (37) but assumes equal equilibrium melting point for the crystalline region in the homopolymer and the blend.

This equation relates the observable  $T_m$  of the homopolymer to that of the blend. The  $T_m^*$  of the homopolymer is still required to take into account the morphological changes in the crystalline blend. The last two terms in this equation disappear for athermal mixtures.

#### CONCLUSION

The spherulitic radial growth rates in a miscible blend of semicrystalline and amorphous polymer are shown to be slower than that of the semicrystalline homopolymer. The half-time crystallization in the blends is higher than that of the homopolymer. The observable melting temperature in a blend is related to the blend's equilibrium melting temperature via four terms, morphology, entropies and enthalpy. The observable melting-point depression in the blend is not easily related to the observable melting temperature of the homopolymer without any simplifying assumption. The present theory requires careful experimental work for verification.

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#### NOTATION

PPO	poly(2,6-dimethylphenylene oxide)
PS	polystyrene
DPS	deuterated polystyrene
PVDF	poly(vinylidene fluoride)
PMMA	poly(methyl methacrylate)
PVME	poly(vinyl methyl ether)
PES	poly(ether sulphone)
PEO	poly(ethylene oxide)
PVC	poly(vinyl chloride)
PBA	poly(butyl acrylate)
PE	polyethylene
CPE	chlorinated polyethylene
PP	polypropylene
PC	polycarbonate
EVA	ethylene vinyl acetate
PVAc	poly(vinyl acetate)
PEEK	poly(ether ether ketone)
PET	poly(ethylene terephthalate)
I <sub>g</sub>	glass transition temperature
$\Delta G_{u}$	GIBD'S free energy difference per mole of
	crystalline unit of the homopolymer (J mol
A 11	of crystalline unit)
$\Delta n_{u}$	heat of menting of the crystalline unit in the homopolymor $(I mol^{-1} of crystalline unit)$
15	$f(x) = \frac{1}{2} \frac{1}{$
$\Delta o_u$	unit)
и	number of crystalline units which is equivalent
	to the lamella thickness
σ.	surface free energy of chain-folded surface
- 6	(J cm <sup>-2</sup> )
$\sigma_{o}$	lateral surface free energy $(J \text{ cm}^{-2})$
$\Delta g_{ m M}$	difference in the free energy of mixing per mole
	of crystalline component (J mol <sup>-1</sup> of crystalline
	component)
$T_{\rm m}$	observable melting point (K)
$T_{\rm m}^*$	equilibrium melting point of the homopolymer
	(K)
G	spherulitic radial growth rate ( $\mu m s^{-1}$ )
α, β	constants
$f_{j}$	free volume fraction
Δα	difference in the thermal expansion coefficients
	(K)
w <sub>c</sub>	volume crystallinity at time t
W <sub>max</sub>	maximum volume crystallinity
N <sub>0</sub>	density of nuclei (nuclei $\mu$ m <sup>-2</sup> )
$\Delta \mu_{2u}$	$(I \text{ cm}^{-3} \text{ mol})$
V.	molar volume of the crystalline unit
$V_{i}^{2u}$	molar volume of the amorphous polymer unit
$\phi_{i}$	volume fraction of component <i>i</i>
$r_i$	chain length of polymer i
. 1	

## Crystallization of a miscible blend: S. Rostami

χ12	Flory–Huggins interaction parameter per
	crystalline unit
$P_2^*$	hard core pressure of component 2
$V_2^{\overline{*}}$	hard core volume of component 2
$\tilde{v}_2$	reduced volume of component 2
ĩ	reduced volume of the blend
$\tilde{P}_2$	reduced pressure of component 2
$\tilde{T}_2^-$	reduced temperature of component 2
$\theta_i^-$	surface site fraction of component i
$X_{12}$	enthalpic interaction energy $(J \text{ cm}^{-3})$
$Q_{12}^{}$	entropic contact energy $(J \text{ cm}^{-3} \text{ K}^{-1})$
$S_i$	surface-to-volume ratio of component i
$\omega_i$	weight fraction of component <i>i</i>

- hard core specific volume ( $cm^3 g^{-1}$ )
- $v^{*}_{isp} \Delta H_{M}$ heat of mixing  $(J g^{-1})$

 $\Delta b_{\rm M}$ partial molar entropy difference

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